Modeling of Power Losses Caused by Hidden Tree-Related High Impedance Faults

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Abstract

The great majority of overhead distribution systems in urban and rural areas of countries such as Australia, Iran and etc., are in interfering with vegetation. This phenomena leads to high impedance faults (HIFs) which not produce enough fault current to be detectable and consequently causes electrical energy losses. In this paper, according to experimental data obtained from measurements, the effective factors in power losses caused by trees are studied and a new numerical model of power loss is presented so as to reflect the effects of environmental conditions and biological classification. The base of this method is according to Samuelson theory. In proposed algorithm, the impacts of species, short-term environmental conditions (temperature and humidity) and long-term environmental conditions (Seasonal variations in physiology) on the power loss estimation are fully considered. Experimental investigations on a real low voltage (380 V) and medium voltage (20 kV) distribution network verify the algorithm’s operation.

Keywords: vegetation-related power loss, high impedance faults (HIFs), distribution system, finite element method, experimental investigations.

1. Introduction

The importance of precise and low time-consuming evaluation of the power losses in systems is becoming increasingly essential to achieve systems with higher efficiency and reliability. A notable part of power losses in distribution systems is related to the growth of vegetation beside power lines. This tree overgrowth near power lines leads to high impedance faults. These faults cannot provide enough current for protective devices. So undetectability and continuity of them causes large energy loss. However, no accurate method for estimation of these losses has been presented thus far. Previous researches in the field of high impedance fault (HIF) have not considered power loss and just focused on detection and location of HIF on medium voltage [1-4]. As shown in table 1, the results of two different researches in HIF current measurement are also incompatible with each other. This shows that tree-related power loss is a variable parameter which depends on different factors. Therefore, due to importance of power losses issue in distribution networks, using the results of precise measurement and accurate estimation of losses considering all effective factors can provide solutions for future decisions.

<table>
<thead>
<tr>
<th>Species</th>
<th>20 kV power line</th>
<th>20 kV power line</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pine</td>
<td>100 mA</td>
<td>0.9 – 2.2 mA</td>
</tr>
</tbody>
</table>

A number of approximation approaches for estimating power losses have been presented in the literature. Numerous studies in the field of numerical estimation of power losses have been done. This kind of estimation was mostly performed for devices with complex geometries. For instance, according to a research work in 2016, due to complex cable’s geometry, ac losses prediction of them can only be achieved by advanced numerical tools. That study used finite-element-based models to compute the ac losses of Roebel cables. Another research work which conducted in 2015, described a numerical approach to determine the magnetic power losses caused by alternating magnetizations in thin electrical steel sheets. A study in 2016 also presented 3-D numerical modeling of ac losses in multi filamentary MgB₂.
cables. The important thing in these approaches is to consider the factors affecting leakage current and consequently power losses. In a research work was conducted in 2006, the leakage current analysis was performed on 20 kV suspension porcelain insulator contaminated by salt moisture. This research showed how the both salty moisture affect the insulator performance and for the long-term the flashover could happened and will leads to a phase to the ground fault. Another research in 2002, studied the resistive leakage current characteristic of MOV surge arresters. In this work, different factors including inner moisture were investigated. A research also investigated the effect of moisture on leakage currents of GRP composite hollow cylinders. The experiments showed a direct correlation between the absorbed moisture and the amount of leakage current. Another study investigated the effect of moisture content on leakage current flow through wooden pole structures. A research work conducted in 2013 presented an approach for determination of moisture in paper insulation of power transformers. In a study in 2014, the temperature distribution and moisture content of an SF-insulated CT was studied by considering current flowing through it [8]. In 1988, the effect of temperature field and moisture content in the vicinity of underground power cables which affect current carrying capacity of buried cables was modeled. In addition to environmental factors, material or species should also be considered in modeling. For instance, according to a study in 2012, electric current flowing through trees changed with the species. Based on measurements taken on the trees touching LV power lines [9], the internal structure of trees and consequently the amount of leakage current passes through them changes in short-term environmental conditions (temperature and humidity) and long-term environmental conditions (seasonal variation in tree physiology). Furthermore, the effect of moisture content variations on electrical resistance is not the same for all species [27]. Considering the factors mentioned above, this research presents a finite element-based algorithm for vegetation-related power loss estimation.

2. Impressibility of Power Losses from Biological Classification

In order to verify the impressibility of power losses from biological classification, several HIF experiments were performed on different species of trees under 20 kV power lines in Hamedan/Iran as show in Figure 1. These species included Ash, Poplar and Walnut. The fault’s current waveform of each species was captured by using a power analyzer that provides a high sampling rate of 1024 samples/period. Stored data were down loaded by laptop.
The obtained results from tree-related HIF tests of different species on MV power lines are documented in figures 2. As shown, under similar environmental conditions, measured fault current values are not same for different species.

![Waveform graphs for a) Walnut Tree, b) Poplar Tree, and c) Ash Tree](image)

Figure 2. Fault’s Current Waveform of Tested Species (mA)

3. Impressibility of Power Losses from Seasonal Variations in Physiology

A series of experiments were carried out in different seasons (spring, summer and autumn) to verify the hypothesis of losses impressionability from the seasonal variations in physiology. The experiments were conducted on-site on live trees grown next to the 380 volt distribution network in Hamendan, Iran. The tested species included Pine, Ash, Plane and Acacia. Figure shows the tested pine tree. Testing Procedure was as follow: Short piece of cooper conductor had touched the power line and providing connection to tree as show in Figure 3. As minimum leakage current was in the 100 nanometer regime, to accurately measure the total leakage flowing to the intended connection, a micrometer measurement device with accuracy of 0.1 μA (Model VC97) had been placed in series with conductor. The variations of leakage current value were studied in different weather and seasonal conditions and summarized in figures 4 to 7.

Broad-leaf trees in terms of vessels are divided into three classes, semi-ring porous species, diffuse porous species and ring porous species. The wood of ring porous species are divided into two categories, spring wood (early wood) with wider vascular channel and thinner vascular wall which formed during spring season, and autumn wood (or late wood) with narrow vascular channel and thicker vascular wall which formed during autumn season. So ring porous trees do not have the same vascular sections during spring and autumn. While there is no significant difference between vascular sections in diffuse porous trees during spring and autumn. Among tested trees, Plane places in diffuse porous group and that is why its vascular
sections in spring, summer and autumn are same. So maximum transferred water in its vessels is same in all seasons. According to this point and with regard to this fact that autumn is the most humid season in Hamadan, it can be concluded that the maximum and minimum leakage current of Plane is occurred in autumn and summer respectively. Unlike the Plane, the transferred water in vessels of Ash and Acacia which placed in ring porous species and consequently their leakage current are maximum and minimum in spring and autumn respectively. In conifers such as Pine, there is no considerable difference between tracheids of spring wood and autumn wood [27]. So, changes in maximum leakage current follow the same pattern of Plane. Test results in figures confirm the above assumptions.

Figure 3. Limb’s Direct Connection to S-Phase of 380 Volt Network (Pine-Test)

Figure 4. Maximum Value of Measured Leakage Current in Tested Pine over Seasons

Figure 5. Maximum Value of Measured Leakage Current in Tested Plane over Seasons
4. Equivalent Moisture Content

Placing a tree in an environment, results in moisture exchange between air and tree. The values for the equivalent moisture content of wood under various combinations of relative humidity and temperature is shown in table 2. According to this table, tree moisture content is a function of temperature and humidity. These values are applicable for all species.

To apply moisture content values of table 1 to proposed algorithm, these values are calculated using the following formula [11].

\[
MC = \frac{1800}{W} \left[ \frac{kh}{1-kh} + \frac{2k_1 k_2 k^2 h^2}{1 + k_1 kh + k_2 k^2 h^2} \right]
\]

(1)

Where, MC and h is respectively moisture content (%) and relative humidity (%/100). For the temperature in degrees Celsius \((T_c)\), Values of \(W\), \(k\), \(k_1\) and \(k_2\) in equation (1) are also obtained using the following relations.

\[
W = 349 + 1.29T_c + 0.01357T_c^2
\]

\[
k = 0.805 + 0.000736T_c - 0.00000273T_c^2
\]

\[
k_1 = 6.27 - 0.00938T_c - 0.000303T_c^2
\]

\[
k_2 = 1.91 + 0.0407T_c - 0.000293T_c^2
\]

(2)
5. The Electrical Resistance of Different Trees

The electrical resistance of trees is affected by several factors, including tree species, temperature and humidity of environment [9]. Therefore, each species has its own electrical characteristics. Figure 8 shows electrical resistance-moisture content characteristics of the sample trees, including pine, spruce, beech, birch, larch and oak.

There have been many studies of this type, in which the linear relationship between the logarithm of electrical resistance of tree with its moisture content is extracted. Logarithmic model used in this paper, is Samuelson model proposed in 1990 that shows the relation between electrical resistance (in mega ohms) with moisture content (in percentage terms) with the following equation.

\[ \log(\log(R) + 1) = a \cdot h + b \]

Where R is the electrical resistance of tree in terms of mega-ohms, a and b are coefficients of the model.

Equation (3) has been proved to be in conformity with experimental data and extensively used in studies of other researchers. Furthermore, the values of coefficients a and b are precisely obtained for different species in numerous studies. For instance, the values of these coefficients for some trees are listed in Table 3.

![Figure 8. Electrical resistance-moisture content characteristics of some tree species [12]](image-url)
6. Electrical Resistance of Softwood and Heartwood of Trees

The internal structure of wood does not have a significant impact on the values of the electrical resistance of the tree. The electrical resistance of the softwood and heartwood of pine measured by these researchers is shown in Figure 9.

Figure 9 shows the correlation between electrical resistance values of sapwood and heartwood. According to these results, difference in moisture content for the same electrical resistance is only 0.5 percent (Table 4). Indeed, at high moisture contents, there is no significant difference between the electrical resistance of sapwood and heartwood. The difference would be notable at low moisture contents. For instance, electrical resistance of the heartwood is two times larger than sapwood at the moisture content of 8%.

Table 3. Regression Coefficients (Samuelsson model) [13]

<table>
<thead>
<tr>
<th>Species</th>
<th>N° samples</th>
<th>Parallel to the grain (Rp)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>a</td>
</tr>
<tr>
<td>Beech</td>
<td>36</td>
<td>-0.046722 ± 0.000579</td>
</tr>
<tr>
<td>Fagus sylvatica</td>
<td>36</td>
<td>-0.046368 ± 0.000597</td>
</tr>
<tr>
<td>European white oak</td>
<td>36</td>
<td>-0.045562 ± 0.000508</td>
</tr>
<tr>
<td>Quercus robur</td>
<td>36</td>
<td>-0.051415 ± 0.000899</td>
</tr>
<tr>
<td>American red oak</td>
<td>36</td>
<td>-0.051567 ± 0.000621</td>
</tr>
<tr>
<td>American ash</td>
<td>36</td>
<td>-0.0393465 ± 0.000775</td>
</tr>
<tr>
<td>Fraxinus sp.</td>
<td>36</td>
<td>-0.07511565 ± 0.001854</td>
</tr>
<tr>
<td>American chestnut</td>
<td>36</td>
<td>-0.0467145 ± 0.001164</td>
</tr>
<tr>
<td>Castanea dentata</td>
<td>36</td>
<td>-0.0480084 ± 0.000790</td>
</tr>
<tr>
<td>Iroko/African teak</td>
<td>36</td>
<td>-0.045967 ± 0.001143</td>
</tr>
<tr>
<td>Chlorophora excelsa</td>
<td>27</td>
<td>-0.0467145 ± 0.001364</td>
</tr>
<tr>
<td>American cherry</td>
<td>35</td>
<td>-0.0480084 ± 0.000790</td>
</tr>
<tr>
<td>Prunus serotina</td>
<td>36</td>
<td>-0.045967 ± 0.001143</td>
</tr>
<tr>
<td>Limba/White afra</td>
<td>35</td>
<td>-0.0480084 ± 0.000790</td>
</tr>
<tr>
<td>Terminalia superba</td>
<td>19</td>
<td>-0.0539734 ± 0.000976</td>
</tr>
</tbody>
</table>

Figure 9. Electrical Resistance Values of Sapwood and Heartwood for Pine [12]
Table 4. Calculated Moisture (a) and Resistance Values (b) for Pine Sapwood and Heartwood

<table>
<thead>
<tr>
<th>Resistance</th>
<th>a) Moisture content, %</th>
</tr>
</thead>
<tbody>
<tr>
<td>10 MOhm</td>
<td>21.0</td>
</tr>
<tr>
<td>1000 MOhm</td>
<td>12.1</td>
</tr>
<tr>
<td>10000 MOhm</td>
<td>9.3</td>
</tr>
<tr>
<td>Moisture content</td>
<td>b) Resistance, MOhm</td>
</tr>
<tr>
<td>8%</td>
<td>32000</td>
</tr>
<tr>
<td>12%</td>
<td>11000</td>
</tr>
<tr>
<td>15%</td>
<td>90</td>
</tr>
</tbody>
</table>

7. Proposed Algorithm to Estimate the Leakage Current in Various Tree Species

It is necessary to consider tree species, short-term environmental conditions (temperature and humidity) and long-term environmental conditions (seasonal variations) in leakage current calculations. To consider long-term environmental conditions in calculations, the tomography imagery of each season will be used. Using tomography imagery, the initial resistivity of tree in each season is obtained. This resistance is assigned to a specific environmental condition by which the initial moisture content of tree (MC0) is achieved. So for each season, there will be an initial resistivity at initial moisture content.

According to Eq 3, the electrical resistance can be calculated based on corresponding moisture content.

\[ R = 10^{0.8 \cdot MC + b - 1} \]  (4)

Values of coefficients of relation 4 are selected according to studied species. According to constant dimensions of tree and based on Eq 4, tree resistivity is proportional to tree electrical resistance.

\[ \rho \propto R \propto 10^{0.8 \cdot MC + b - 1} \]  (5)

Regarding Eq 5 and initial resistivity derived from tomography images (\( \rho_1 \)) and according to moisture content of tree, resistivity value corresponding to specified environmental conditions is estimated using the following equation. This obtained resistivity is applied to finite element analysis as input data and the power loss of tree is calculated (Figure 10).

\[ \rho_2 = \frac{\rho_1 \cdot 10^{MC2 \cdot b - 1}}{10^{MC1 \cdot b - 1}} \]  (6)
For finite element analysis, tree trunk structure is assumed as two concentric truncated cones and boundary conditions are specified as voltage and current density of conductors and the ground voltage.

From Maxwell’s equation [14],

$$\nabla \cdot E = -\nabla^2 V + \mu \frac{\partial^2 V}{\partial t^2}$$

(7)

$$J = -\sigma E$$

(8)

$$\nabla^2 J - \mu \sigma \frac{\partial J}{\partial t} = 0$$

(9)

Where $\mu$ is the magnetic permeability, $\sigma$ is the electrical conductivity. Assuming sinusoidal excitation with an angular frequency $\omega$ and thus substituting

$$\nabla \cdot E = -\nabla^2 V + \mu \frac{\partial^2 V}{\partial t^2}$$

(10)

yields the J-formulation in the frequency domain to solve eddy current problems:

$$\nabla^2 J - j \omega \mu \sigma J = 0$$

(11)

By employing the electric potential and considering the problem of three dimensions in Cartesian system of coordinates ($x, y, z$), hence:

$$\frac{\partial}{\partial x} \left( \frac{1}{\mu} \frac{\partial J}{\partial x} \right) + \frac{\partial}{\partial y} \left( \frac{1}{\mu} \frac{\partial J}{\partial y} \right) + \frac{\partial}{\partial z} \left( \frac{1}{\mu} \frac{\partial J}{\partial z} \right) - j \omega \mu \sigma J = 0$$

(12)

The governing equation of each 4-node tetrahedron element is directly derived from the Maxwell’s equations and solved using Galerkin approach [15].

7. Power Loss Estimation of Cupressus Touching 20 kV Power Line Based on the Proposed Algorithm

A 20 kV single core copper conductor XLPE insulated power cable has touched the power line and providing connection to tree (Figure 11). As minimum leakage current was in the millimeter regime, to accurately measure the total leakage flowing to the intended connection, current probe of power analyzer with resolution of 0.1 mA (Model Prova 6830A+6801) has been closed around the cable.

This experiment was done on live Cupressus Sempervirens tree grown next to 20 kV feeder. Figure 12 shows the test procedure. Figure 13 displays the captured waveform of high impedance fault current on the scope. As shown in waveform hardcopy, the RMS value of current is 0.635 amps. This RMS value is related to environment with humidity of 65.5 % and temperature of 28.5°C.
Electrical properties of internal tissues of Cupressus Sempervirens trunk have been determined using tomographic cross section (Figure 14). The colors in the tomogram in Figure 14 represent the 2-dimensional distribution of electric resistivity in Ω m where dark blue shows the lowest and dark red the highest measured electric resistivities. The x- and y-axes of the tomogram indicate the dimension of the stem slice in meter.

To evaluate the performance of proposed algorithm, estimated leakage current values using algorithms were compared to the values obtained from experiments. According to Figure 14, the amount of resistivity with corresponding moisture content of 11.1 percent is about 68 ohm meters. This resistivity was applied to FEM model as input data and leakage current and power loss value were obtained as output data. Figure 15 shows the estimated and measured value of electrical leakage current of Cupressus Sempervirens tree for FEM analysis.
Figure 15. Leakage Current Through the Cupressus (Ampere)
(Tests Conducted in the Summer, 28.5 °C, 65.5 %)

The figure 16 indicates the calculated value of tree power loss using finite element method for various combinations of relative humidity and temperature of spring. As shown in figure 16, at higher levels of humidity, power loss rate is abruptly increased.

Figure 16. Power Losses Variations of Cupressus Touching MV Power Line under Different Environments of Summer

8. Power Loss Estimation of Pine Touching 380 V Power Line Based on the Proposed Algorithm

To evaluate the performance of proposed algorithm, estimated leakage current values using algorithms were compared to the values obtained from experiments. According to Figure 17, the amount of resistivity with corresponding moisture content of 6.8% is about 450 ohm.

Figure 17. Results of Electrical Tomography of Pine at Moisture Content of 6.8 percent in the Spring [17]
Figure 18 shows the estimated and measured value of electrical leakage current for FEM analysis. The difference between the measured and the estimated value of leakage current on figure 18.a and 18.b is respectively about 2 and 24 %.

Figure 18.a. spring, 19°C, 41%  
Figure 18.b. spring, 19°C, 45%  
Figure 18. Leakage Current Through the Pine (Micro Ampere)

Figure 19 indicates tree power loss in Watts for various combinations of relative humidity and temperature of spring.

Figure 19. Power Losses Variations of pine under different environments of spring

9. Conclusion
One of the main problems with the vegetation-related power losses estimation, are impressibility of power losses from numerous factors. In this paper a new methodology for vegetation-related losses estimation in distribution systems was presented so as to reflect the impacts of all effective factors. The methodology used numerical techniques in order to approach accurate model for power losses. The results obtained from the proposed methodology were very close to those obtained from experiments.
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References